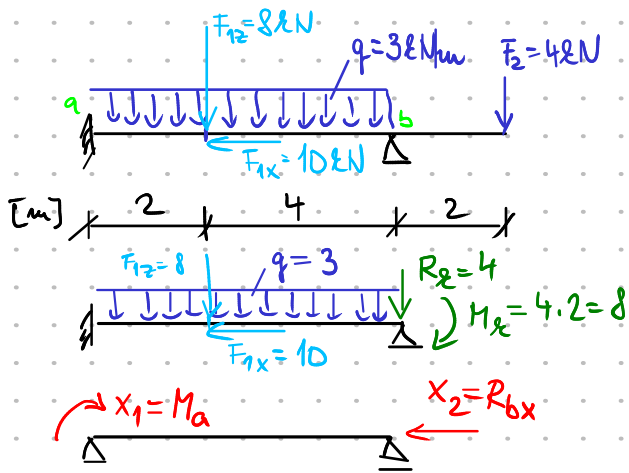
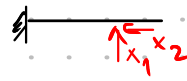




1) $m_s = 2x$



2)

odebra'm staticky určité části konstrukce (konzola, převislý konec) a nahrazen' interakcemi R_2 a M_2

3) podmínky

$\phi_{ab} = 0$ ve větknutí platí nulové
pootočení

$$U_b = 0$$

2 rovnice (nezávislé) o dvou neznámých

3a) vliv osového zatížení

$$U_b: \delta_{20} + \delta_{22} \cdot X_2 = 0 \quad \delta = \int \frac{N\bar{N}}{EA} dx$$

$$\delta_{22} = \frac{1}{EA} [1 \cdot 6 \cdot (1)] = \frac{6}{EA}$$

$$\delta_{20} = \frac{1}{EA} [10 \cdot 2 \cdot (1)] = \frac{20}{EA}$$

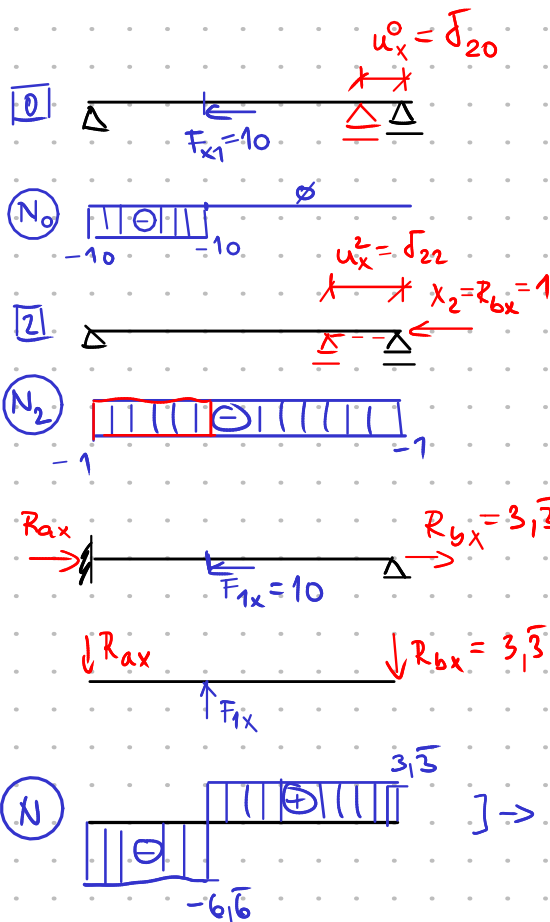
$$X_2 = - \frac{\delta_{20}}{\delta_{22}} = - \frac{20}{6} = -3,33 \text{ kN} = R_{bx}$$

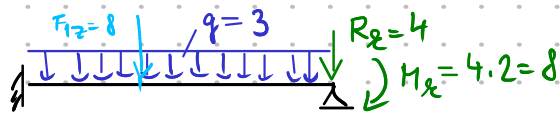
- analogie s řešením ①

$$\sum M_{ai} = 0 \quad (+ \uparrow)$$

$$F_{1x} \cdot 2 - R_{bx} \cdot 6 = 0$$

$$R_{bx} = \frac{20}{6} = 3,33 \text{ kN}$$





3b) řešení příčného zatížení

$$\phi_{ab} = 0$$

$$\phi_{ab} + \alpha_{ab} \cdot M_a = 0 \quad (\delta_{10} + \delta_{11} X_1 = 0)$$

$$\alpha_{ab} = |5.13a| = \frac{1}{3} \frac{l}{EI} = \frac{2}{EI}$$

$$\phi_{ab} = \phi_{ab}^{F_{12}} + \phi_{ab}^q + \phi_{ab}^{M_2}$$

$$\phi_{ab}^{F_{12}} = |5.8a| = \frac{F_{ab}}{6EI l} (l+b) = \frac{8 \cdot 2 \cdot 4}{6EI \cdot 6} (6+4) = \frac{17.7}{EI}$$

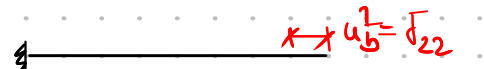
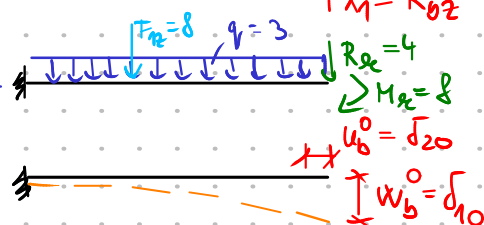
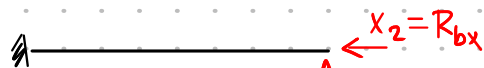
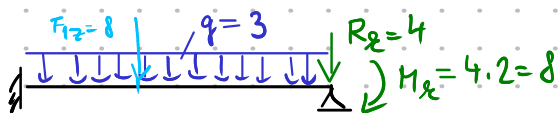
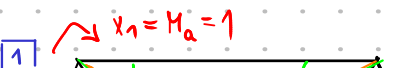
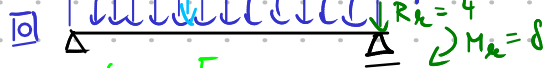
$$\phi_{ab}^q = |5.14a| = \frac{q l^3}{24EI} = \frac{3 \cdot 6^3}{24 \cdot EI} = \frac{27}{EI}$$

$$\phi_{ab}^{M_2} = |5.12b| = \frac{M l}{6EI} = \frac{8 \cdot 6}{6EI} = -\frac{8}{EI}$$

$$\phi_{ab} = \frac{17.7 + 27 - 8}{EI} = \frac{36.7}{EI}$$

$$\frac{36.7}{EI} + \frac{2}{EI} X_1 = 0 \quad | \cdot EI$$

$$X_1 = -\frac{36.7}{2} = -18.38 \text{ kNm}$$



3) řešení konzola

3a) viz předchozí

3b) $W_b = 0$

$$W_b^0 + W_b^1 \cdot X_1 = 0 \quad (\delta_{10} + \delta_{11} X_1 = 0)$$

$$W_b^1 = |14.1|2| = \frac{F l^3}{3EI} = \frac{1 \cdot 6^3}{3EI} = \frac{72}{EI}$$

$$W_b^0 = F_{12} W_b^0 + q W_b^0 + R_2 W_b^0 + M_2 W_b^0$$

$$R_2 W_b^0 = |14.1|2| = \frac{F l^3}{3EI} = \frac{4 \cdot 6^3}{3EI} = \frac{288}{EI}$$

$$q W_b^0 = |14.1|5| = \frac{q l^4}{8EI} = \frac{3 \cdot 6^4}{8EI} = \frac{486}{EI}$$

$$M_2 W_b^0 = |14.1|13| = \frac{M l^2}{2EI} = \frac{8 \cdot 6^2}{2EI} = \frac{144}{EI}$$

$$F_{12} W_b^0 = |14.1|1| = \frac{F a^2}{6EI} (3l-a) = \frac{8 \cdot 2^2}{6EI} (3 \cdot 6 - 2) = \frac{85.3}{EI}$$

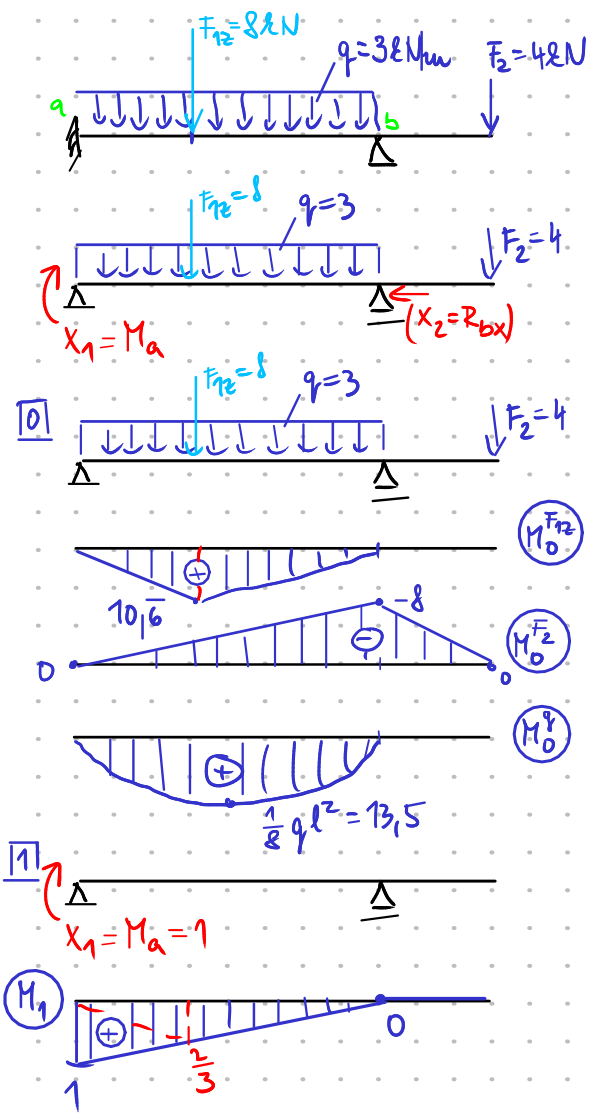
$$W_b^0 = \frac{288 + 144 + 85.3 + 486}{EI} = \frac{1003.3}{EI}$$

$$R_{b2} = -\frac{W_b^0}{W_b^1} = -\frac{1003.3}{-72} = +13.935 \text{ kN}$$

3) klasická silová metoda

3a) viz předešlá

3b)



$$\delta_{10} + \delta_{11} X_1 = 0$$

$$\delta = \frac{1}{EI} \int M \bar{M} dx$$

$$\delta_{11} = \frac{1}{EI} \left[\frac{1}{2} \cdot 6 \cdot 1 \cdot \left(\frac{2}{3} \cdot 1 \right) \right] = \frac{2}{EI} = \delta_{ab}$$

$$\delta_{10} = \delta_{10}^q + \delta_{10}^{F_{12}} + \delta_{10}^{F_2}$$

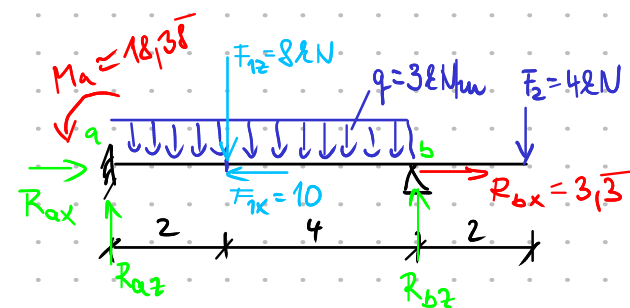
$$\delta_{10}^q = \frac{1}{EI} \left[+ \frac{2}{3} \cdot 13,5 \cdot 6 \cdot \left(\frac{1}{2} \cdot 1 \right) \right] = \frac{24}{EI} = \varphi_{ab}^q$$

$$\delta_{10}^{F_{12}} = \frac{1}{EI} \left[+ \frac{1}{2} \cdot 10,6 \cdot 2 \cdot \left(\frac{1}{3} \cdot 1 \right) + \frac{1}{2} \cdot 10,6 \cdot 2 \cdot \left(\frac{2}{3} \cdot \frac{2}{3} \right) + \frac{1}{2} \cdot 10,6 \cdot 4 \cdot \left(\frac{2}{3} \cdot \frac{2}{3} \right) \right]$$

$$= \frac{14,4}{EI} = \varphi_{ab}^{F_{12}}$$

$$\delta_{10}^{F_2} = \frac{1}{EI} \left[- \frac{1}{2} \cdot 6 \cdot 1 \cdot \left(\frac{1}{3} \cdot 8 \right) \right] = - \frac{8}{EI} = \varphi_{ab}^{F_2}$$

$$\delta_{10} + \delta_{11} X_1 = 0 \Rightarrow X_1 = -18,38 \text{ kNm} = M_a$$



4) vykreslení vnitřních sil

$$\sum F_{xi} = 0 \Rightarrow R_{ax} = +6,6 \text{ kN}$$

$$\sum M_{ai} = 0 \oplus$$

$$M_a - F_{12} \cdot 2 - (q \cdot 6) \cdot 3 + R_{bz} \cdot 6 - F_2 \cdot 8 = 0$$

$$R_{bz} = 13,935 \text{ kN} \quad (\text{viz } x_2 \uparrow)$$

$$\sum M_{bi} = 0 \Rightarrow R_{az} = 16,065 \text{ kN}$$

$$\text{kontrola: } \sum F_{zi} = 0 \quad \checkmark$$